

FACTOR FORM OF A QUADRATIC EXPRESSION

FRI 15 FEB 2019

$$f(x) = a \underbrace{(x-d)}_{\text{This is one factor}} \underbrace{(x-e)}_{\text{This is the other factor}}$$

The word factor means
We are dealing with a
PRODUCT

It's called FACTOR FORM because it is
the product, that is, the multiplication, of 3 terms
a, (x-d) & (x-e).

You can also see the factor form as this

$$f(x) = a(x+r)(x+s) \quad \begin{array}{l} x+(-7) = \\ = x-7 \end{array}$$

EXAMPLES

$$g(x) = 3(x-7)(x+2) = a(x-d)(x-e)$$

Find $a, d, \& e$: $a=3$ $e=-2$
 $d=7$

Find $r \& s$: $r=-7$ $s=2$

FROM STANDARD FORM TO FACTOR FORM

$$f(x) = ax^2 + bx + c = a(x+r)(x+s)$$

Example

$$f(x) = x^2 - 7x + 12 = a(x+r)(x+s) = \boxed{(x-4)(x-3)}$$

Find 2 #'s r & s such that the add to -7 & their product is 12

$$A = -4 \quad B = -3$$

$$\begin{array}{l|l} r+s = -7 & a=1 \\ rs = 12 & \end{array}$$

~~$$\begin{array}{r} 7 \quad 0 \\ -6 \quad -1 \\ 1 \quad 2 \\ \hline -4 \quad -3 \end{array}$$~~

Examples (cont.)

$$f(x) = 2x^2 + 5x - 3 = a(x+r)(x+s)$$

Ans. $a=2$ Hence we need to find two
#s A & B such that

$$A + B = 5$$

$$AB = 2(-3) = -6$$

$$f(x) = \underbrace{(2x-1)}_{2x^2+6x-x-3} (x+3)$$

~~$\begin{matrix} 7 & -2 \\ 6 & -1 \end{matrix}$~~

$$\begin{aligned} A &= 6 \\ B &= -1 \end{aligned}$$

$$f(x) = \underline{3}x^2 + 12x - \underline{15} = (3x + t)(x + u)$$

Ans $A + B = 12$

$$AB = 3 \cdot (-15) = -45$$

$$\begin{array}{r} \cancel{17} - 5 \\ \hline 15 - 3 \end{array}$$

$$A = 15$$

$$B = -3$$

Hence

$$f(x) = (3x + B)(x + \frac{A}{3})$$

$$= (3x - 3)(x + 5)$$

$$= \underline{3(x-1)(x+5)}$$

$$g(x) = \underline{2}x^2 - 13x - \underline{7}$$

Ans:

$$A + B = -13$$

$$AB = 2 \cdot (-7) = -14$$

$$\begin{pmatrix} -14 & 1 \end{pmatrix}$$

$$A = -14 \quad \text{Hence}$$

$$B = 1$$

$$g(x) = (2x + 1)(x - 7)$$

ASSIGNMENT 1 (TERM 3) (DUE: ~~FRI~~ 22nd Feb)

Pages: 139 - 142 Exercises: 3 - 16

ASSIGNMENT 2

Pages: 149 - 151 Exercises: 1 - 14